

# 1 Node description

Let  $T \subseteq A$  be a spanning tree in  $D$ , and consider some node  $v \in V \setminus \{0\}$ . There is an unique (undirected) path, denoted by  $P(v)$ , defined by  $T$  from  $v$  to the root node 0. The arc in  $P(v)$ , which is incident to  $v$ , is called the **basic arc** of  $v$ . The other terminal node  $u$  of this basic arc is called the **predecessor (node)** of  $v$ . The basic arc of  $v$  is called **upward (downward)** oriented if  $v$  is the tail (head) node of its basic arc. If  $v$  is the predecessor of some other node  $u$ , we call  $u$  a **child (node)** of  $v$ . Given some order of all childs of  $v$ , and let  $u$  and  $w$  be two different childs of  $v$ . If  $u$  is smaller than  $w$  with respect to the given order, we call  $u$  the **left sibling** of  $w$  and  $w$  the **right sibling** of  $u$ . If there is no child  $u$  being smaller (greater) than a given child  $w$ , then  $w$  has no left (right) sibling. Each node has at most one child reference, the other children of a node can be reached by traversing the sibling links. The number of nodes in  $P(V)$  is called the **subtree size** of  $v$ .

The subtree size and predecessor variables are used by the ratio test. The orientation, child, and sibling variables are used for the computation of the node potentials. Figure 1 shows a small example of a rooted basis tree for our data structures (the underlying network is a copy from [?]).

node	0	1	2	3	4	5	6	7	8
subtree size	9	8	5	2	1	1	1	2	1
predecessor	nil	0	1	2	3	3	2	1	7
child	1	2	3	4	nil	nil	nil	8	nil
right sibling	nil	nil	7	6	5	nil	nil	nil	nil
left sibling	nil	nil	nil	nil	nil	4	3	2	nil
orientation	-	down	down	up	down	down	down	up	up

Figure 1: Rooted basis tree.